

DEAL: Data-Efficient Active Learning for regression under drift

A First Method Aimed at the Gap of Regression Active Learning with Drift

By Béla H. Böhnke, **Edouard Fouché**, and Klemens Böhm



Overview

- Problem Statement
 - Stream Regression
 - Active Learning for Regression
 - Active Learning for Regression under Drift
- Related Work
- Our Method
- Evaluation
- Outlook

Problem Statement



Related Work



Our Method



Evaluation

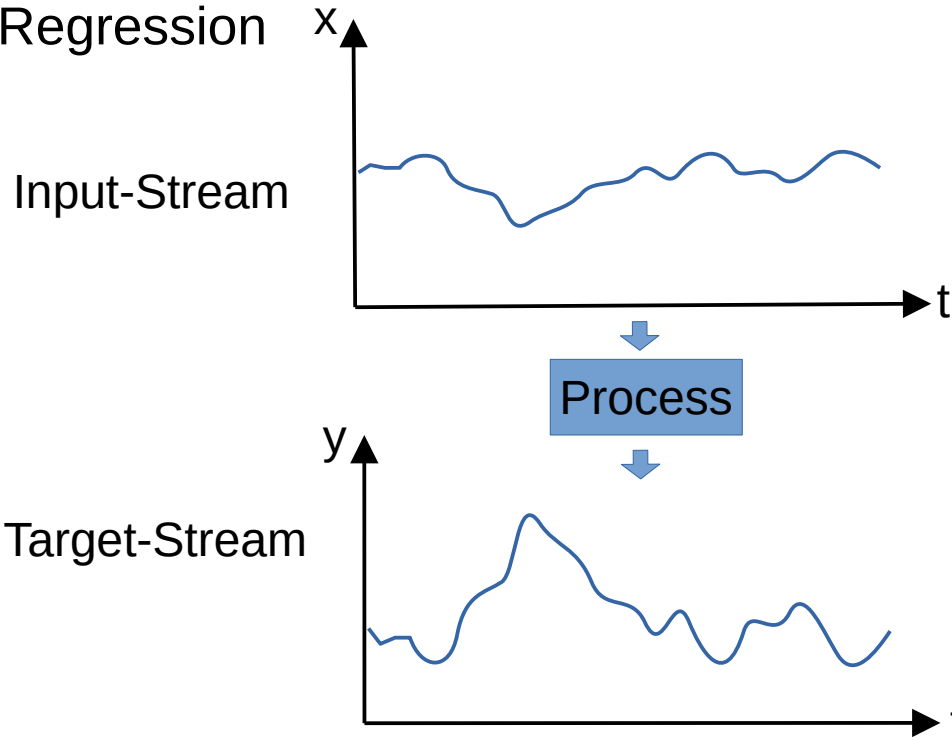


Outlook



Problem Statement

■ Stream Regression



Problem Statement



Related Work



Our Method



Evaluation



Outlook



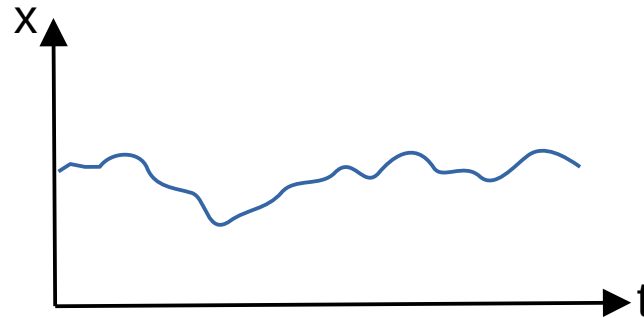
Problem Statement

Stream Regression

Example:

Industrial process control

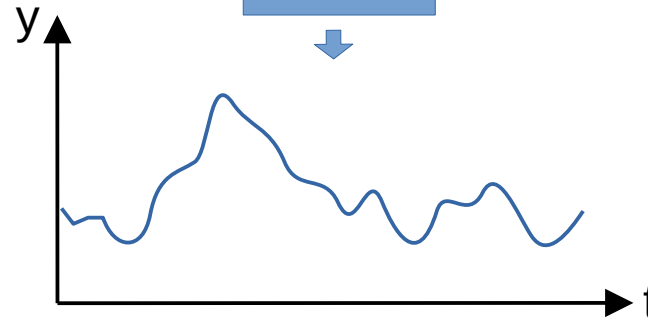
Input-Stream



Process



Target-Stream



Problem Statement



Related Work



Our Method



Evaluation



Outlook



Problem Statement

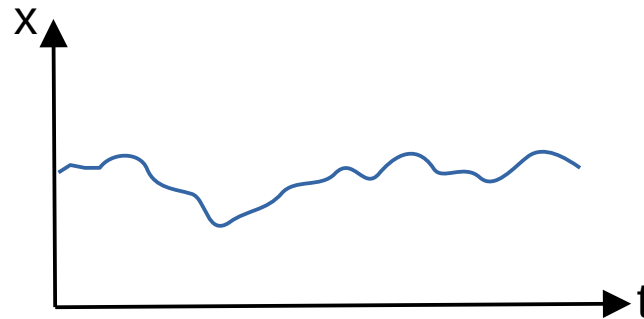
Stream Regression

Example:

Industrial process control

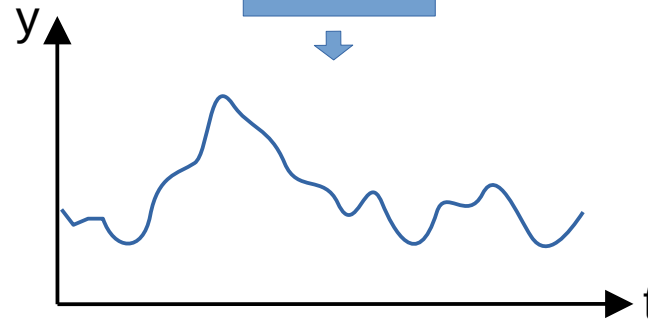
Input-Stream

Process parameters like
pressure, temperature
and materials



Process

Target-Stream



Problem Statement



Related Work



Our Method



Evaluation



Outlook



Problem Statement

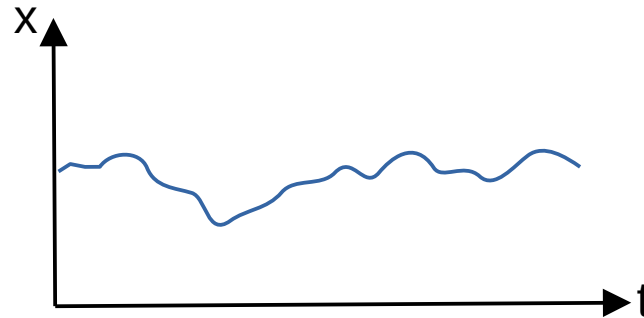
Stream Regression

Example:

Industrial process control

Input-Stream

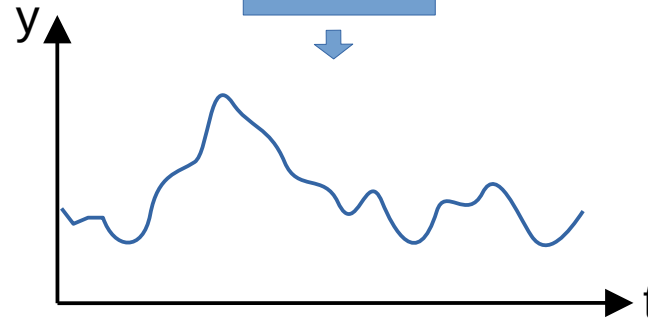
Process parameters like
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Process

Target-Stream

Product quality



Problem Statement



Related Work



Our Method



Evaluation

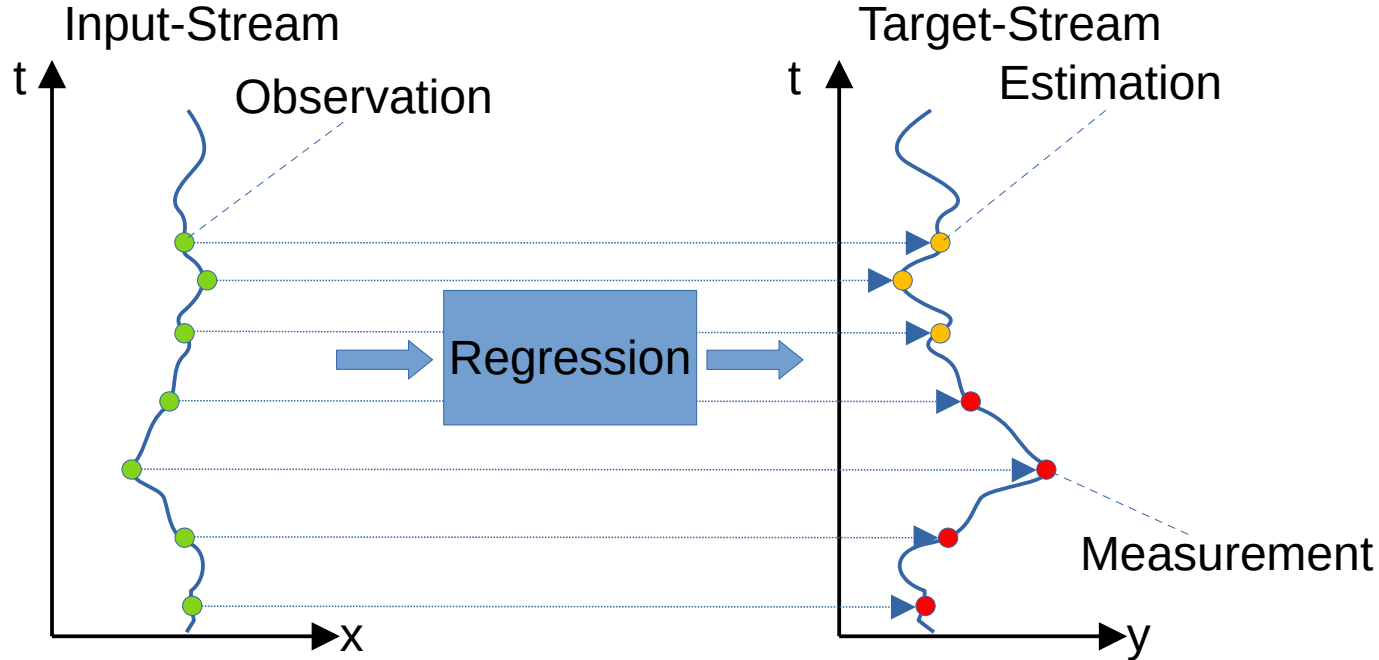


Outlook



Problem Statement

■ Stream Regression



Problem Statement



Related Work



Our Method



Evaluation

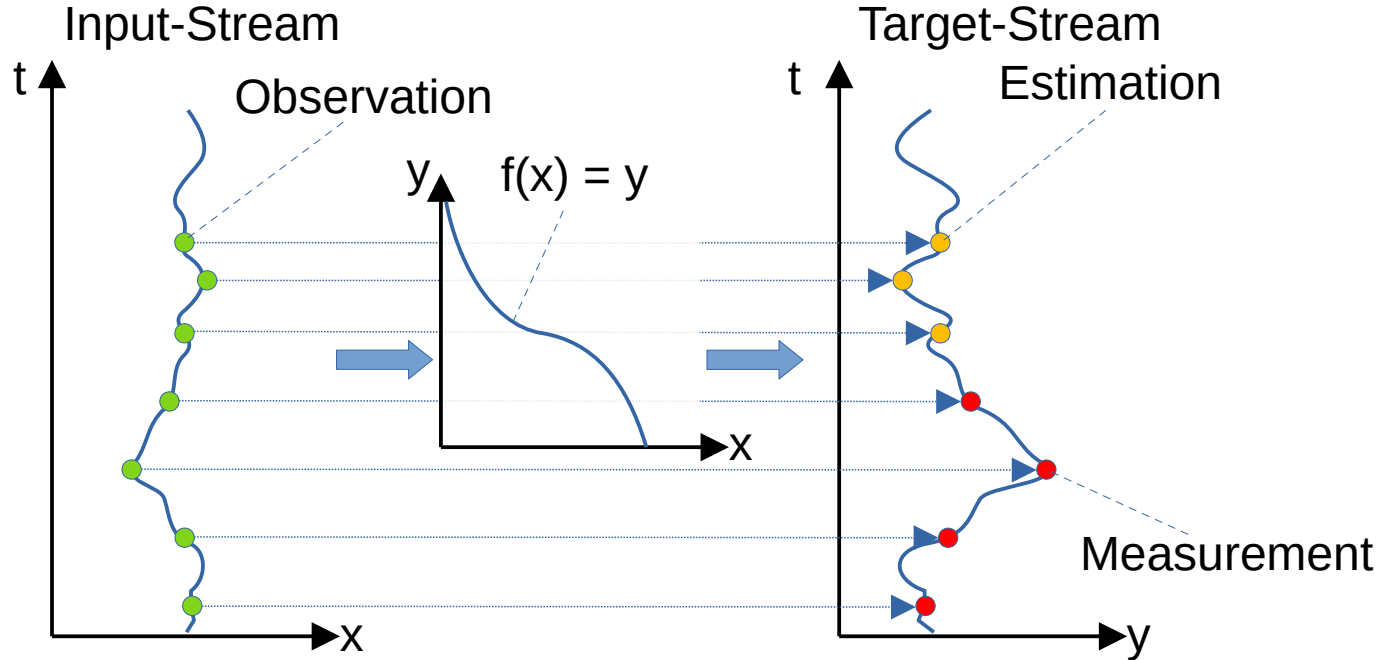


Outlook



Problem Statement

Stream Regression



Problem Statement



Related Work



Our Method



Evaluation

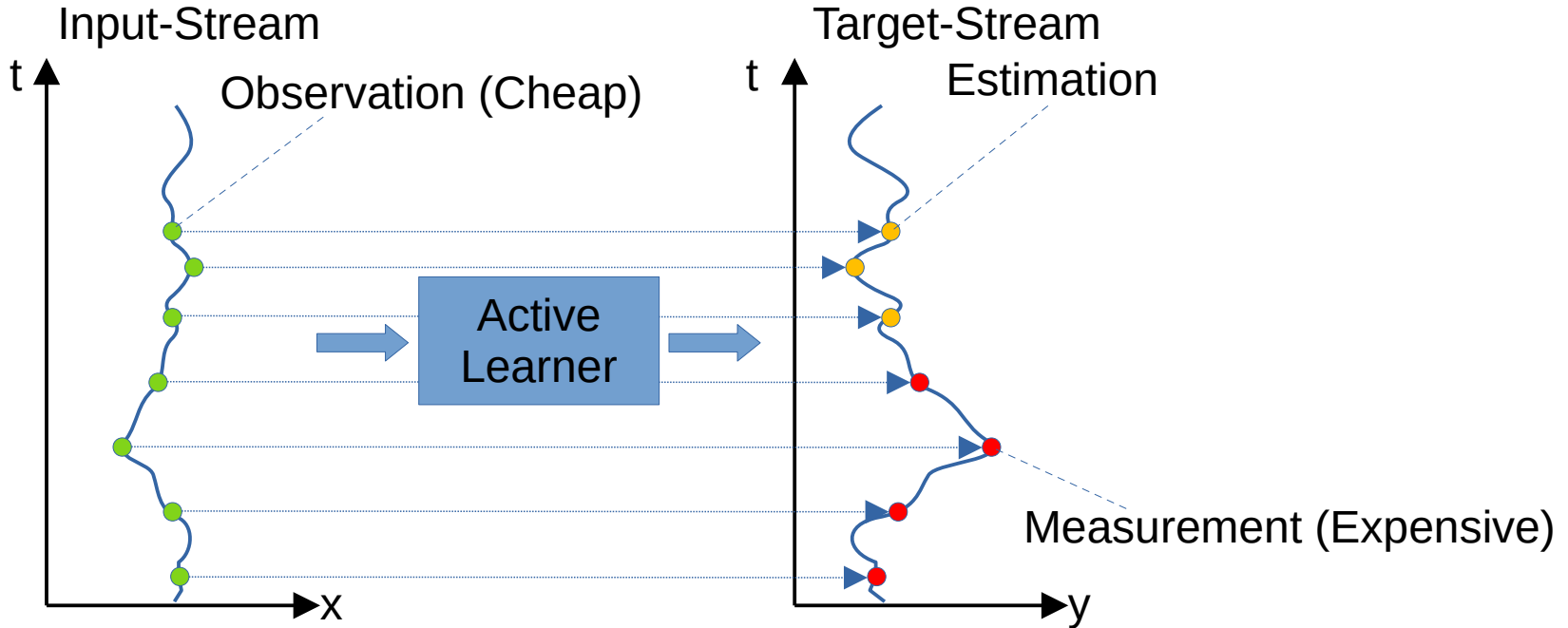


Outlook



Problem Statement

■ Active Learning for Regression



Problem Statement



Related Work



Our Method



Evaluation

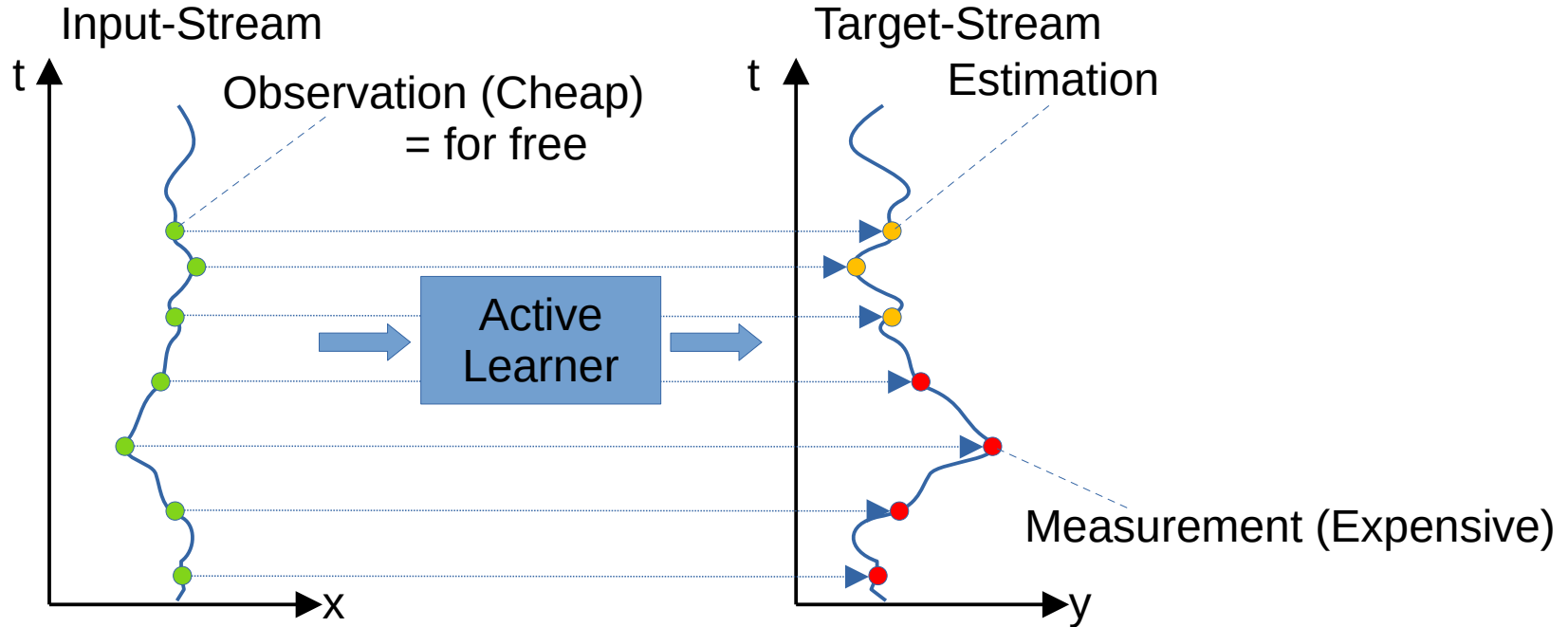


Outlook



Problem Statement

Active Learning for Regression



Problem Statement



Related Work



Our Method



Evaluation

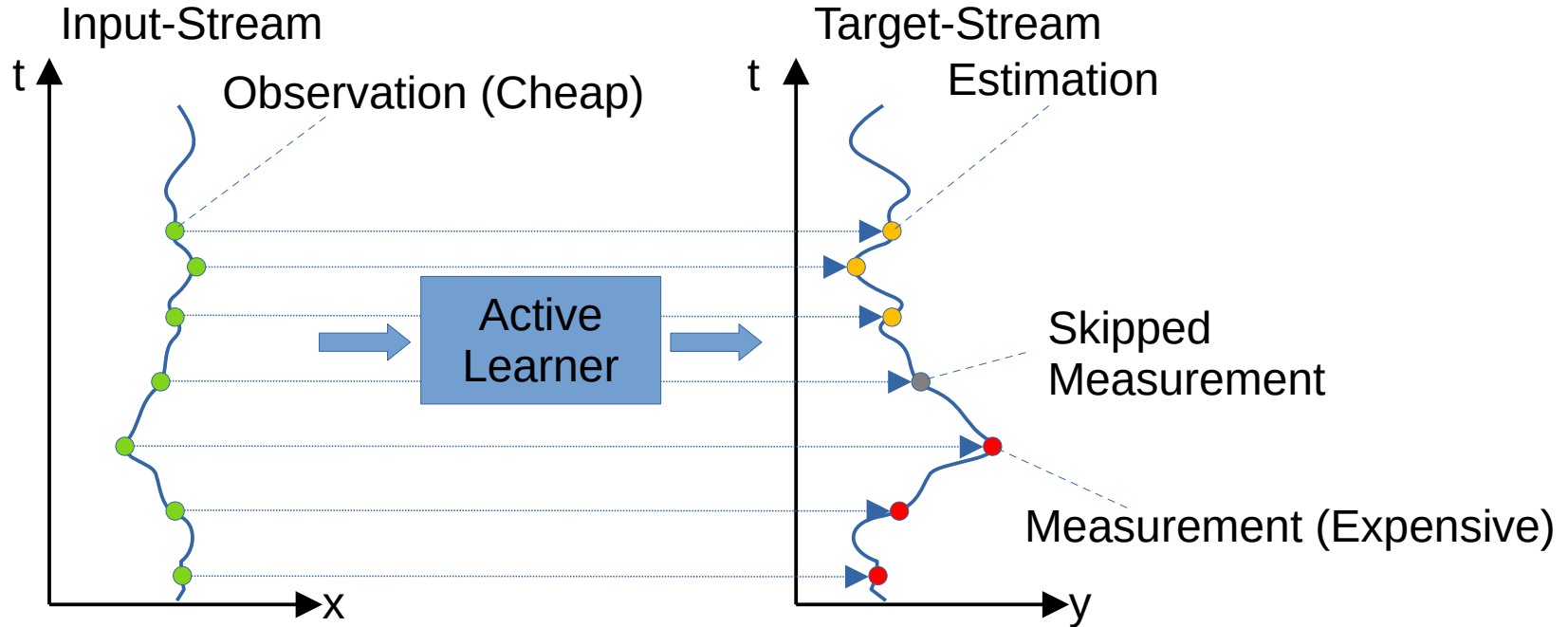


Outlook



Problem Statement

Active Learning for Regression



Problem Statement



Related Work



Our Method



Evaluation

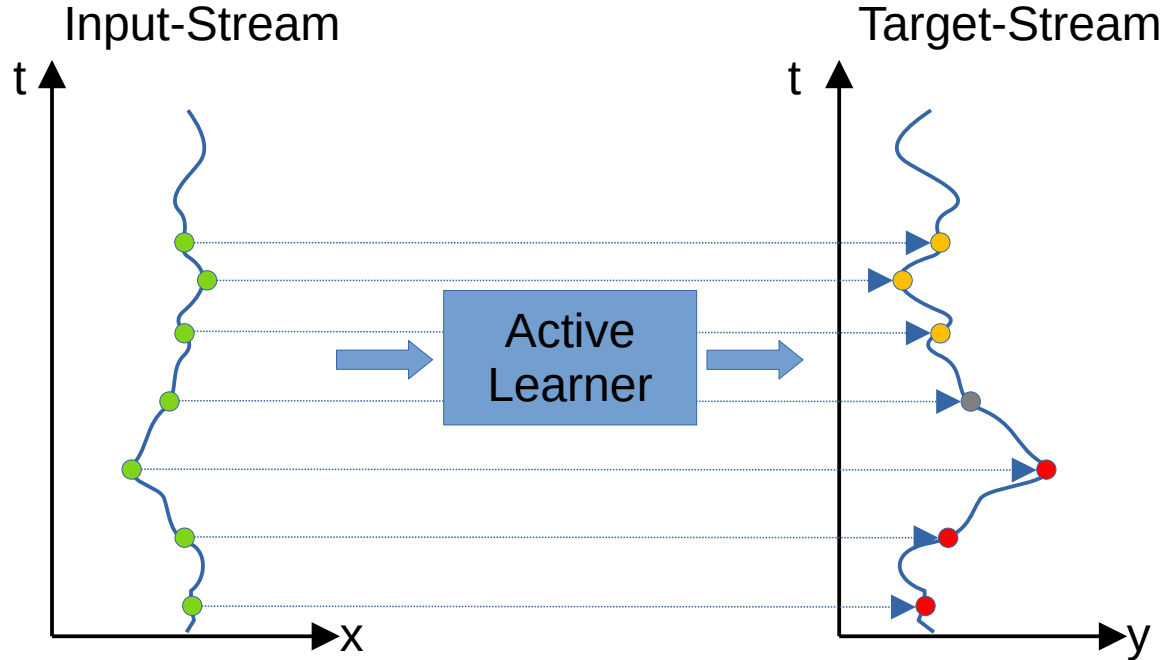


Outlook



Problem Statement

Active Learning for Regression



- Observation (Cheap)
- Measurement (Expensive)
- Skipped Measurement
- Estimation

Problem Statement



Related Work



Our Method



Evaluation

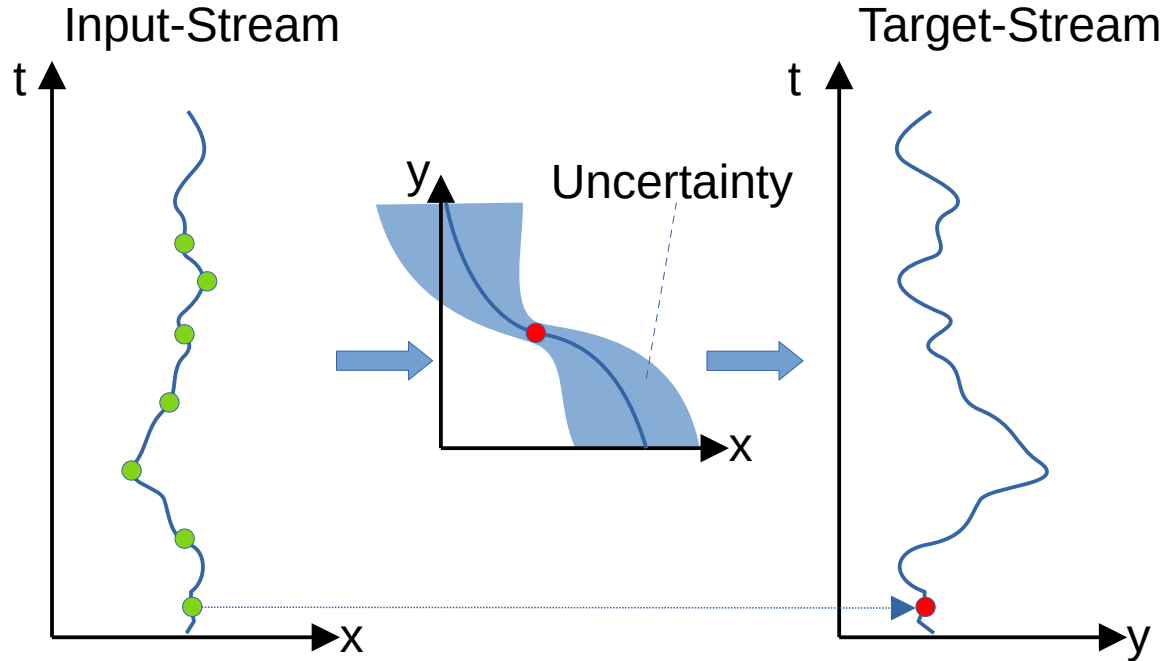


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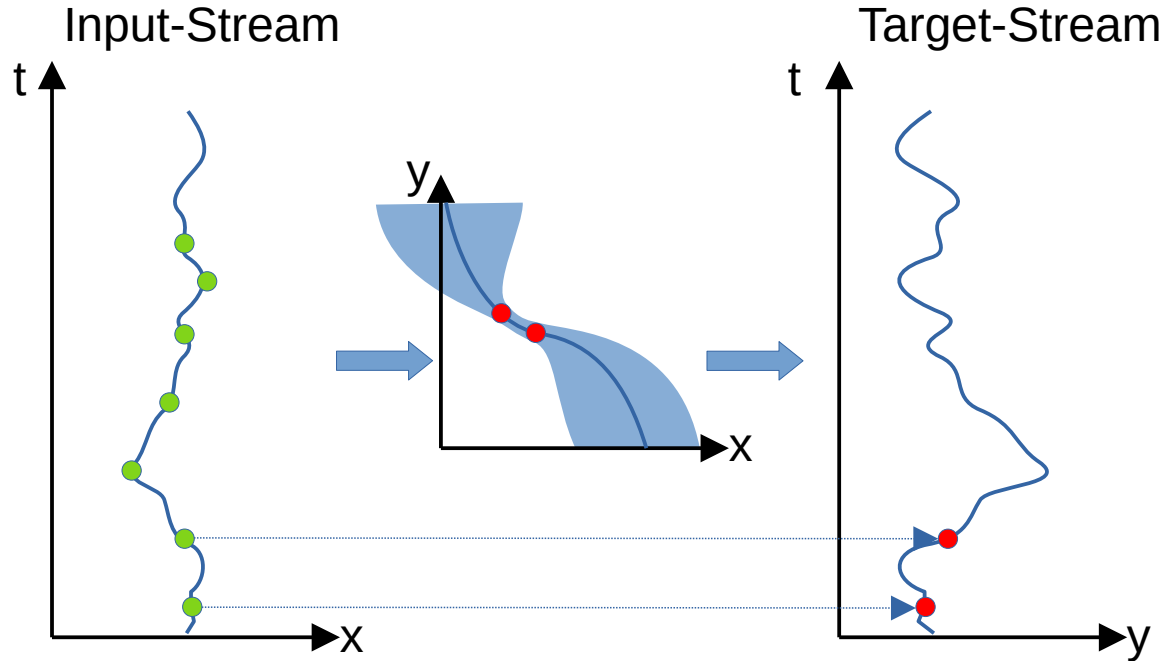


Outlook



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Problem Statement

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Evaluation

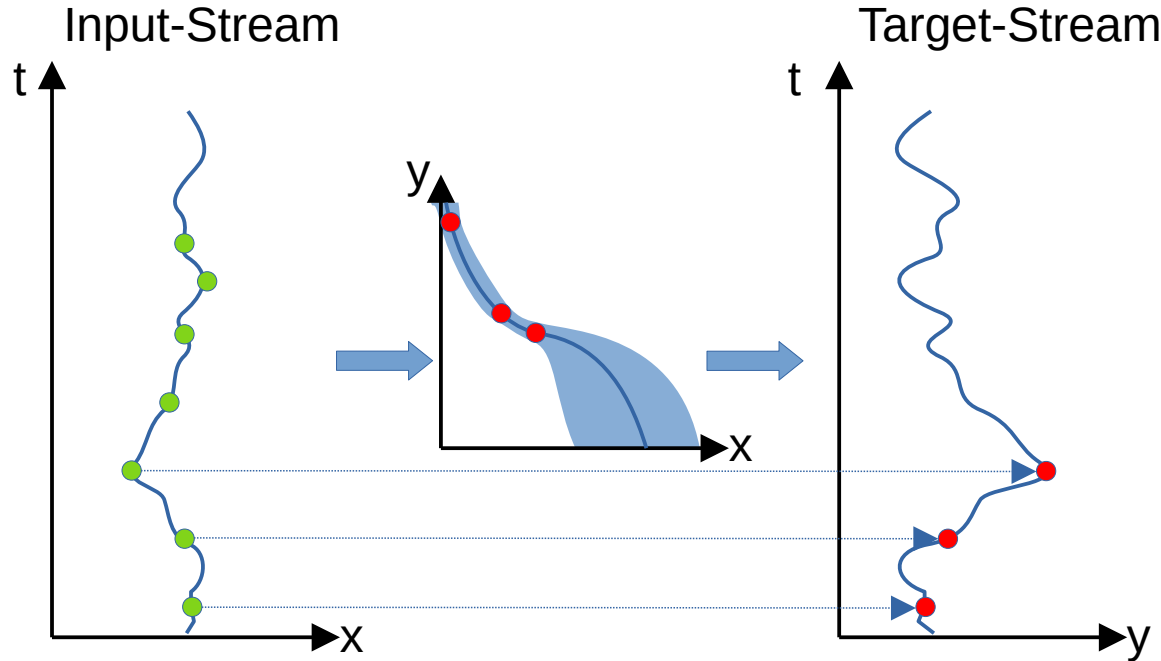
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Evaluation

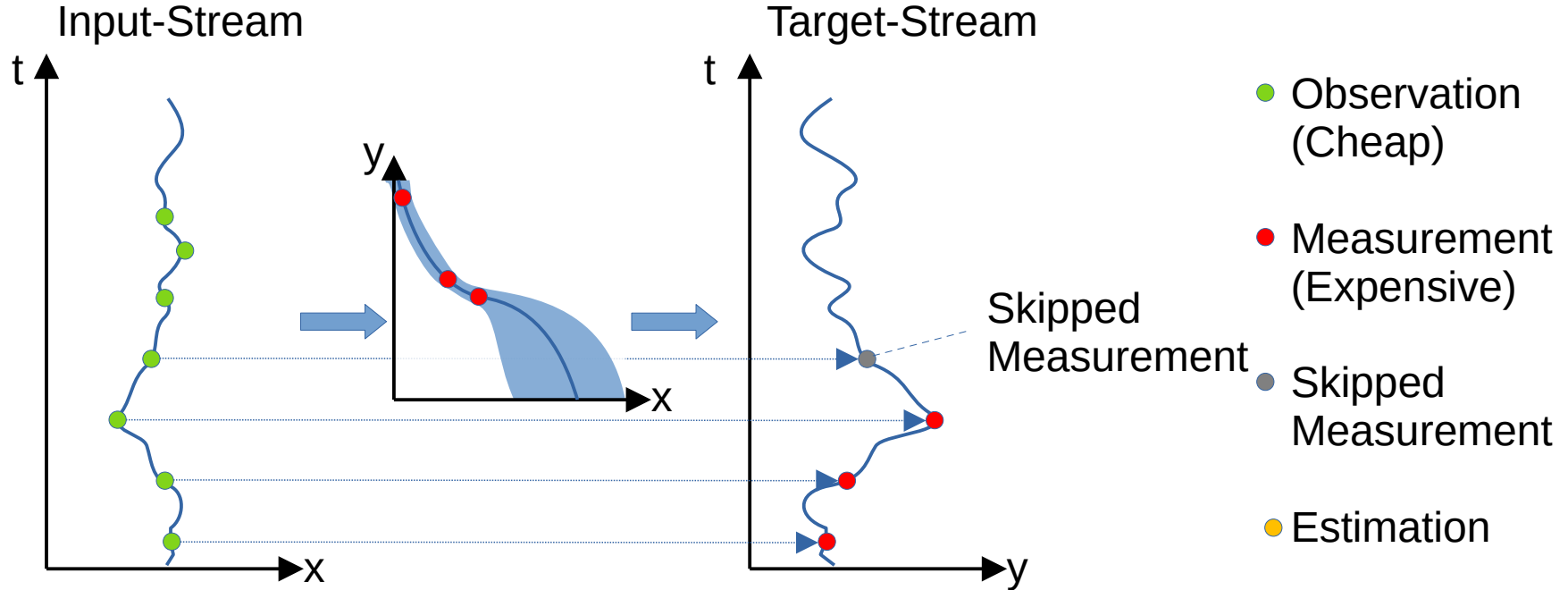


Outlook



Problem Statement

Active Learning for Regression



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Evaluation

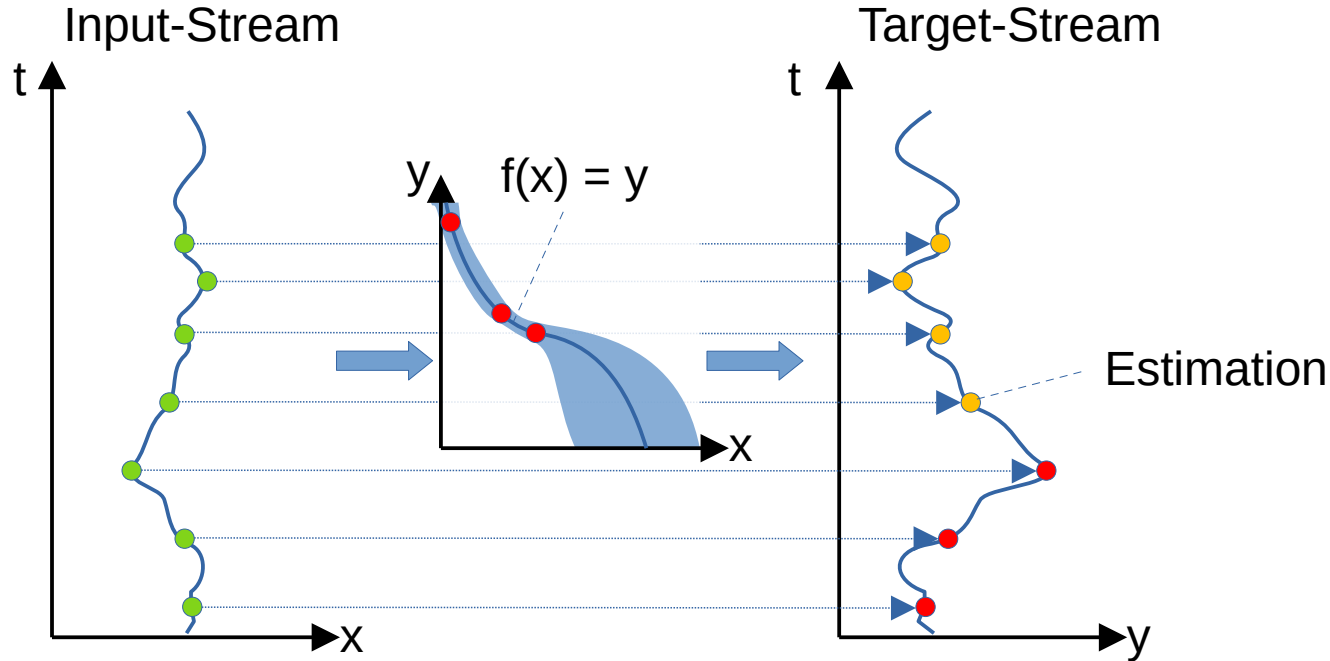
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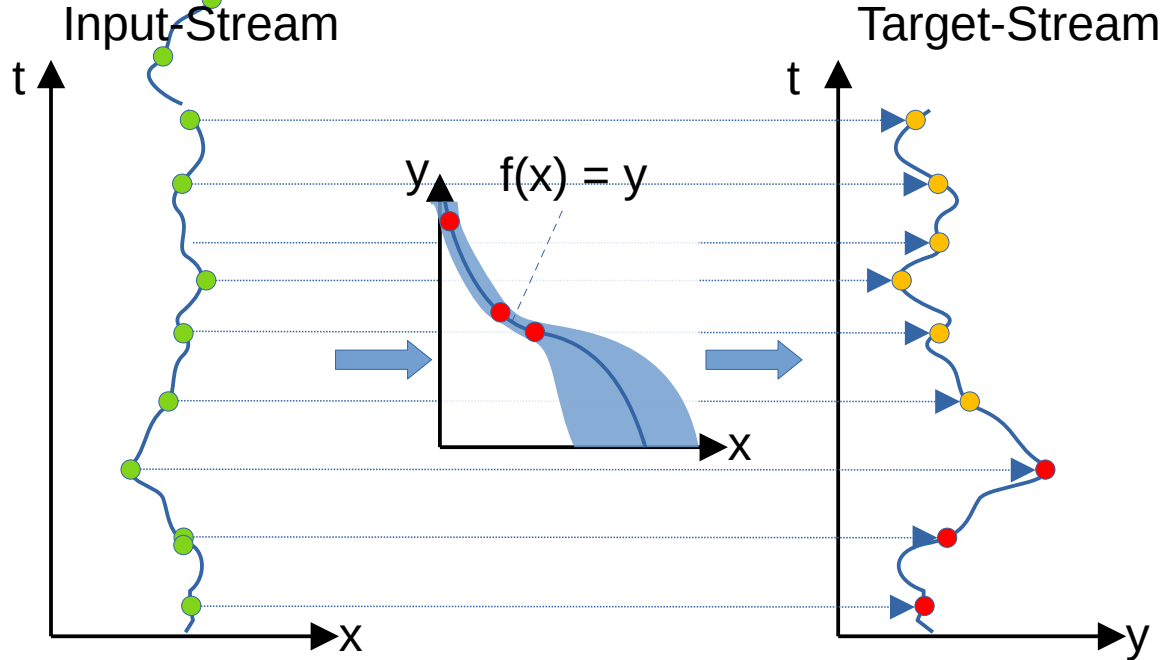


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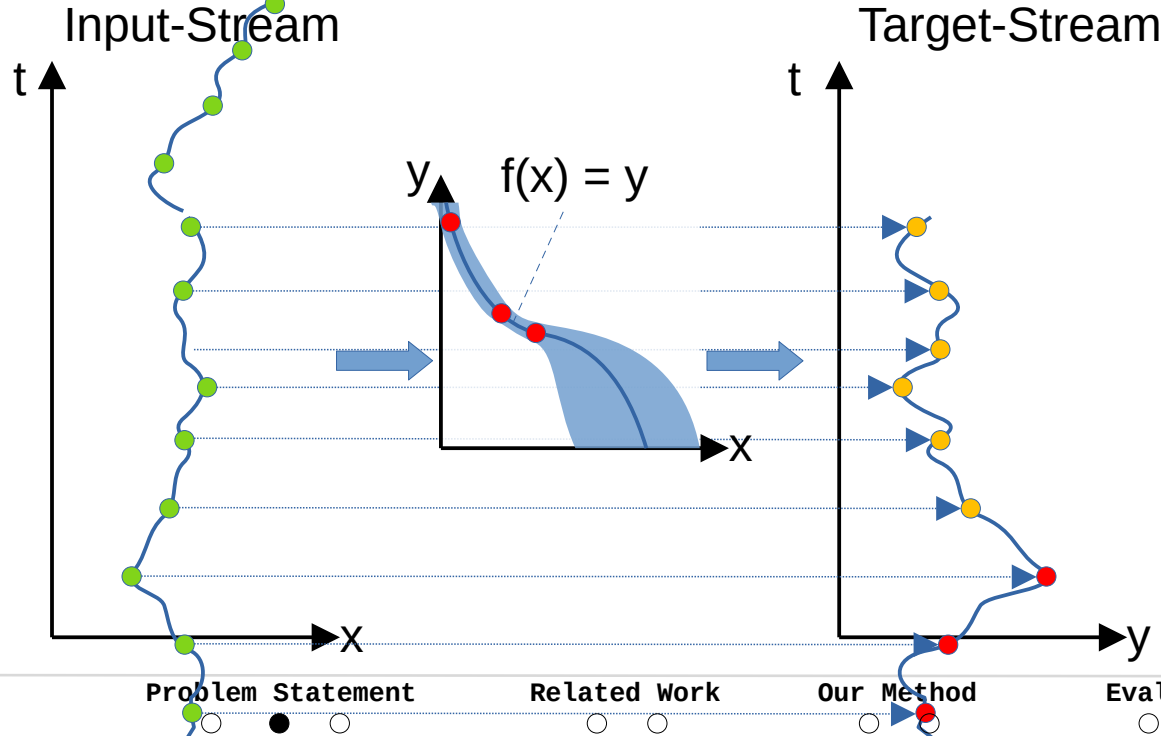


Outlook



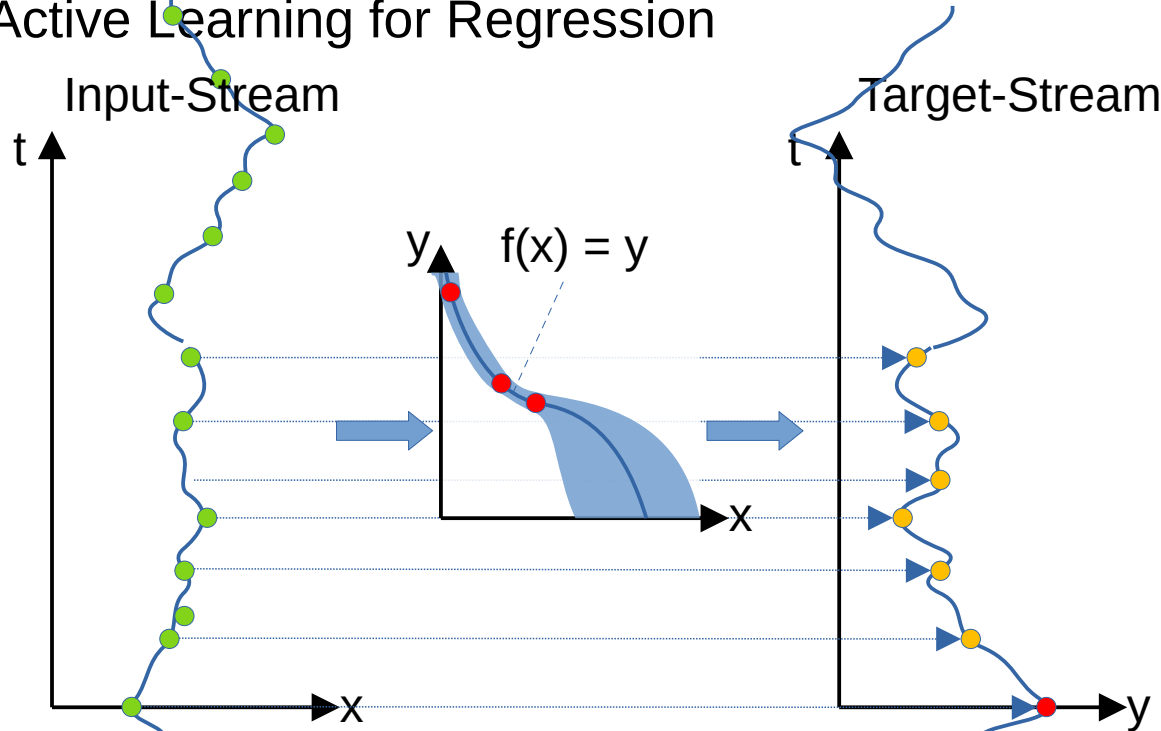
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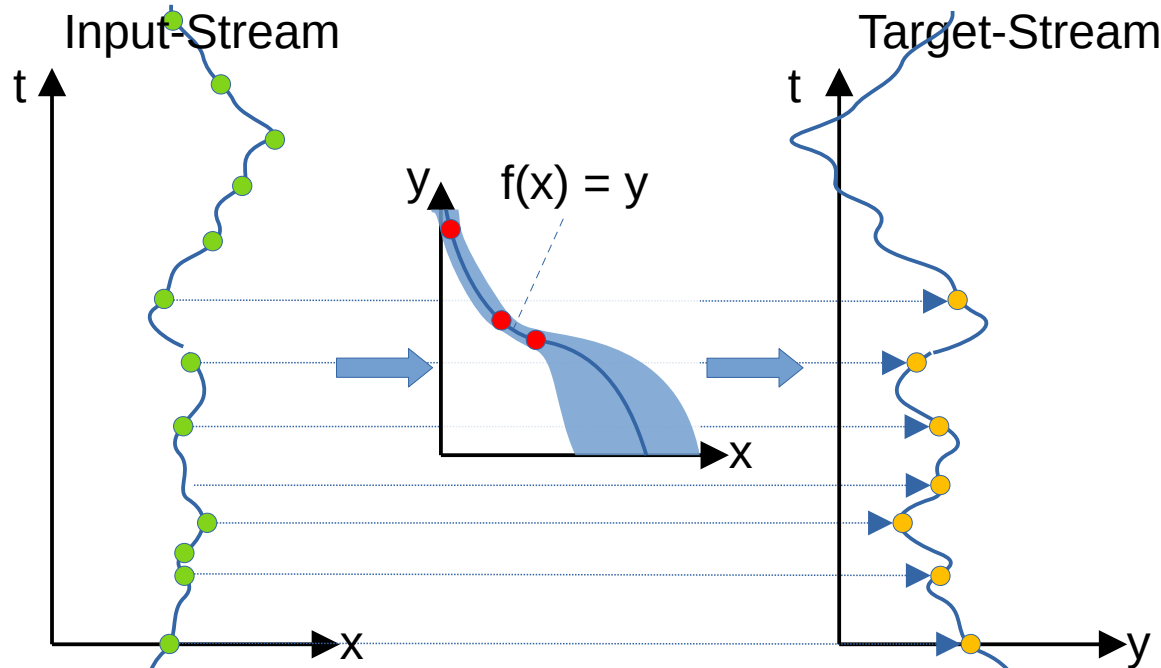
Evaluation

Outlook



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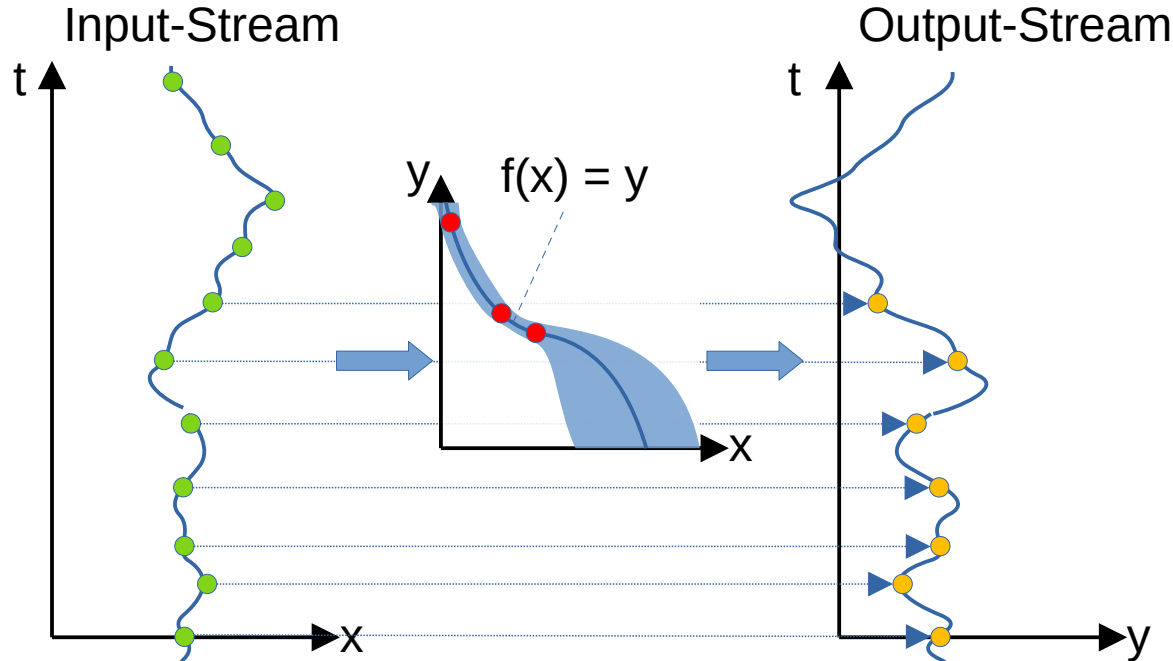
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Problem Statement

Active Learning for Regression



Problem Statement

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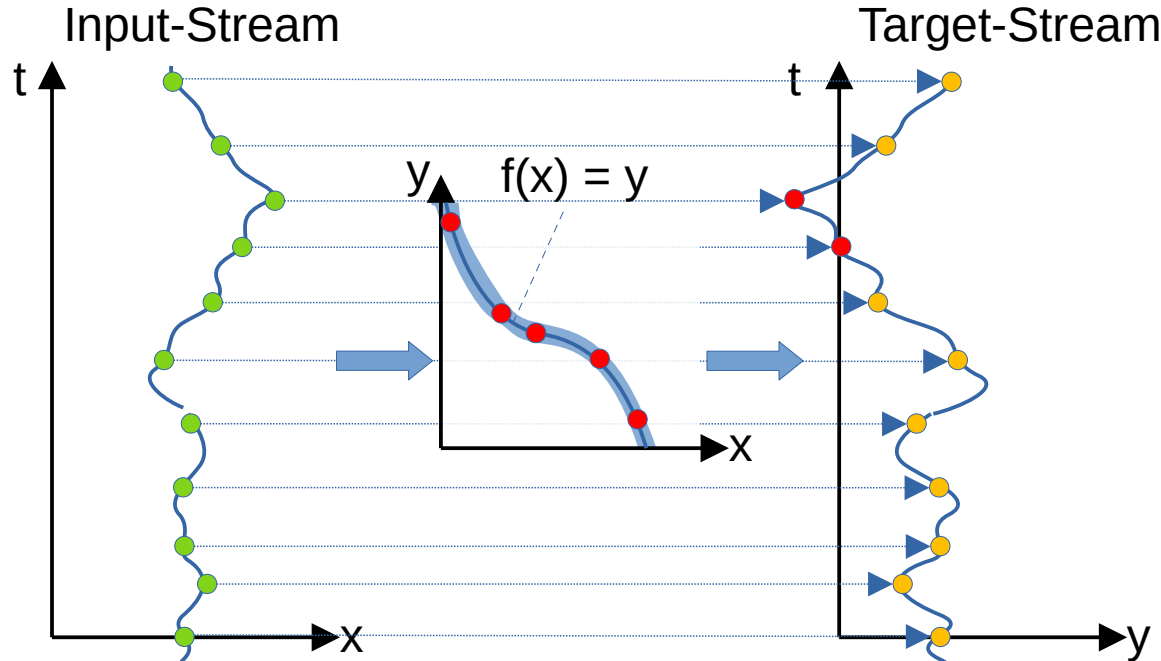
Our Method

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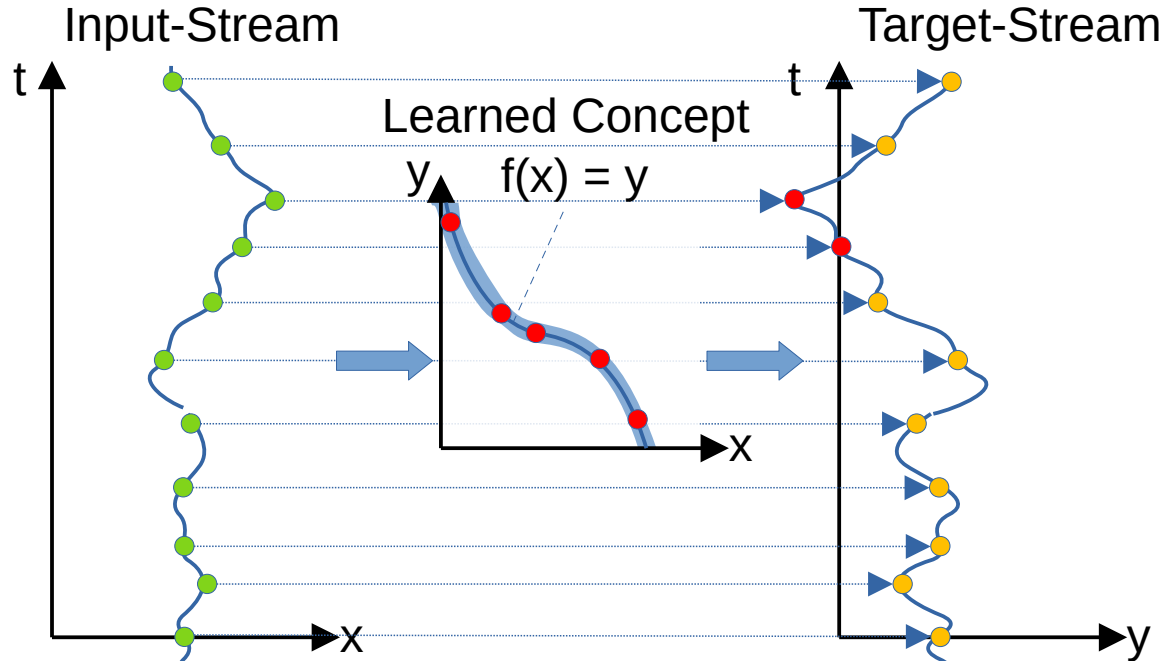
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Problem Statement

Active Learning for Regression



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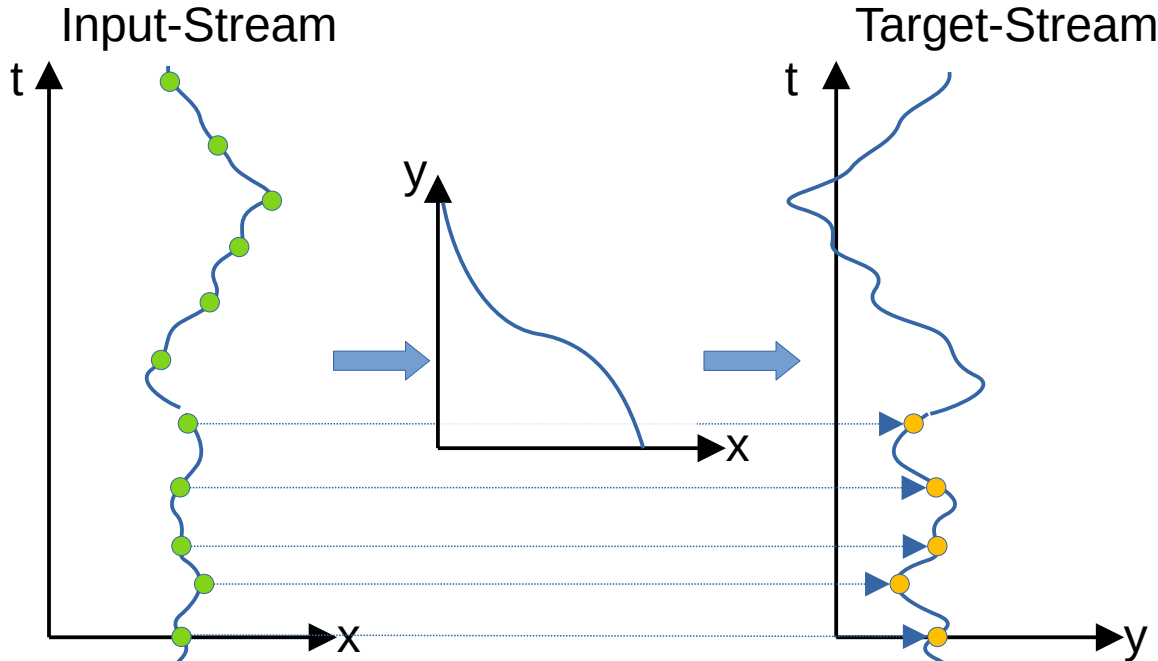
Evaluation

Outlook



Problem Statement

■ Concept Drift



Problem Statement

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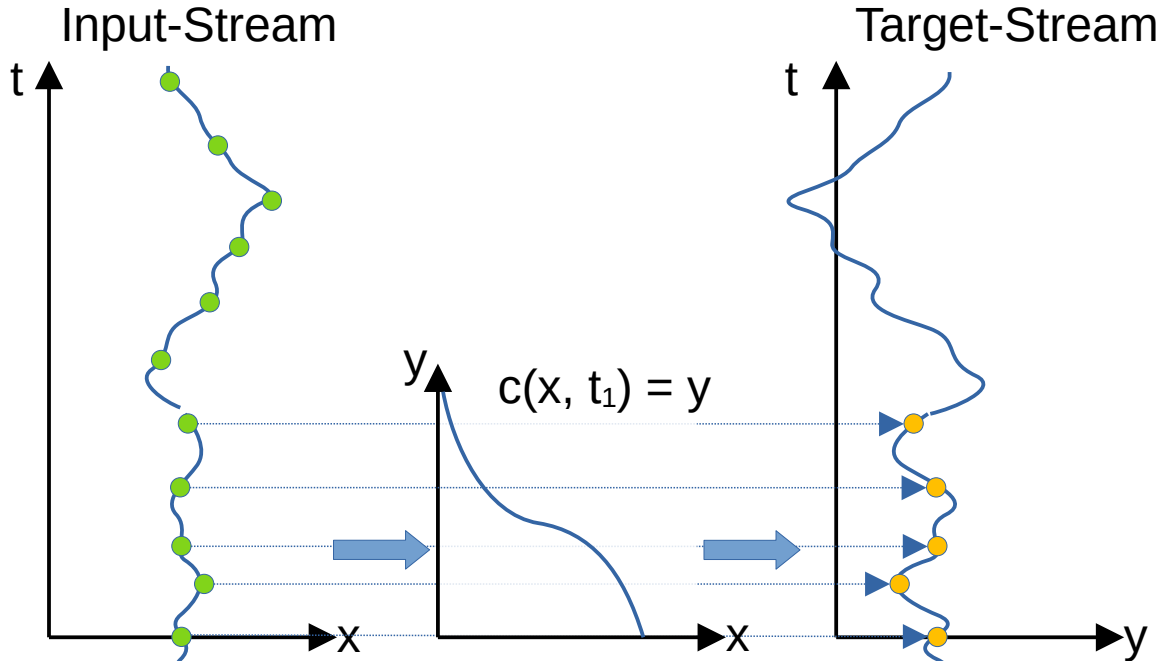
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Problem Statement

■ Concept Drift



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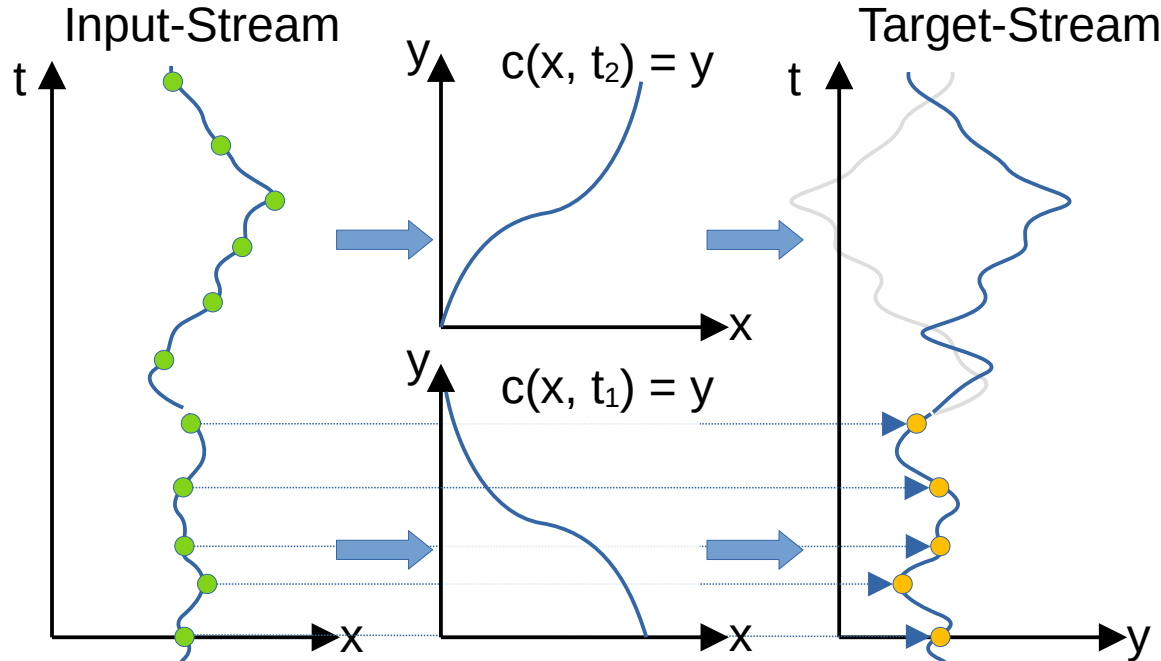
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Problem Statement

■ Concept Drift



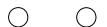
Problem Statement

Related Work

Our Method

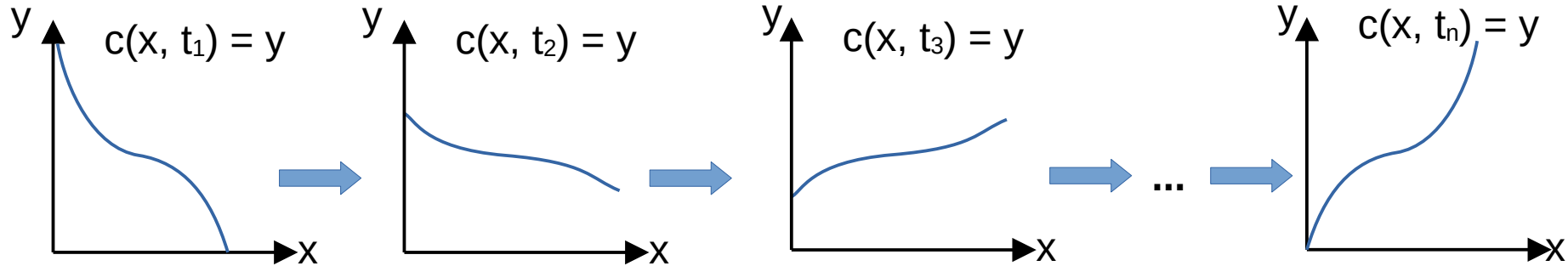
Evaluation

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Problem Statement

■ Concept Drift



Problem Statement



Related Work



Our Method



Evaluation

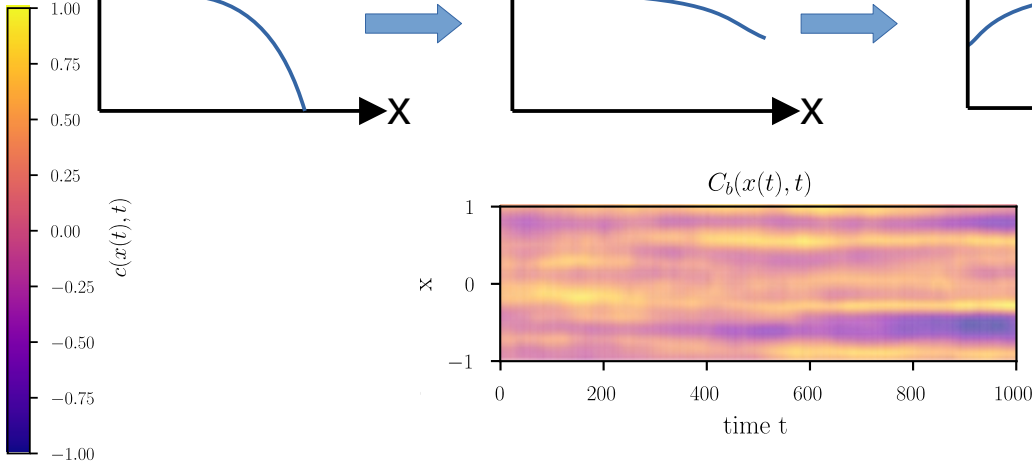
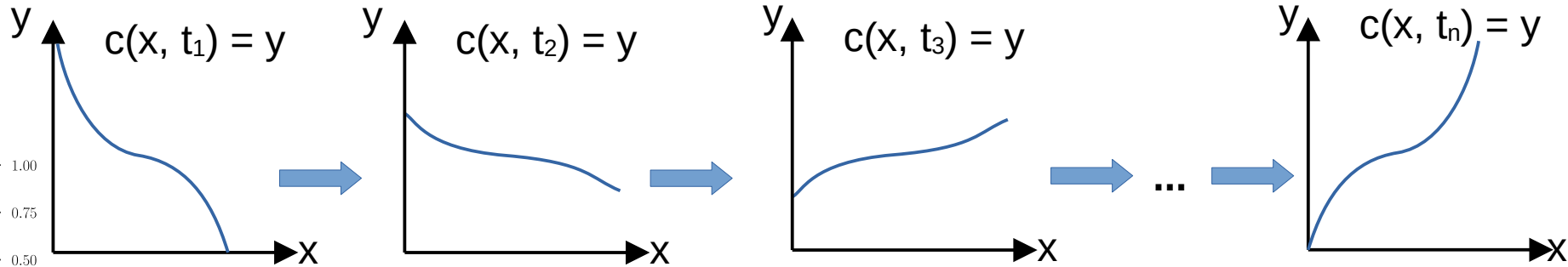


Outlook



Problem Statement

■ Concept Drift



Problem Statement



Related Work



Our Method



Evaluation

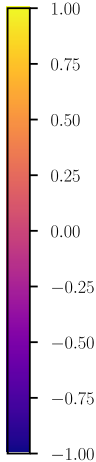
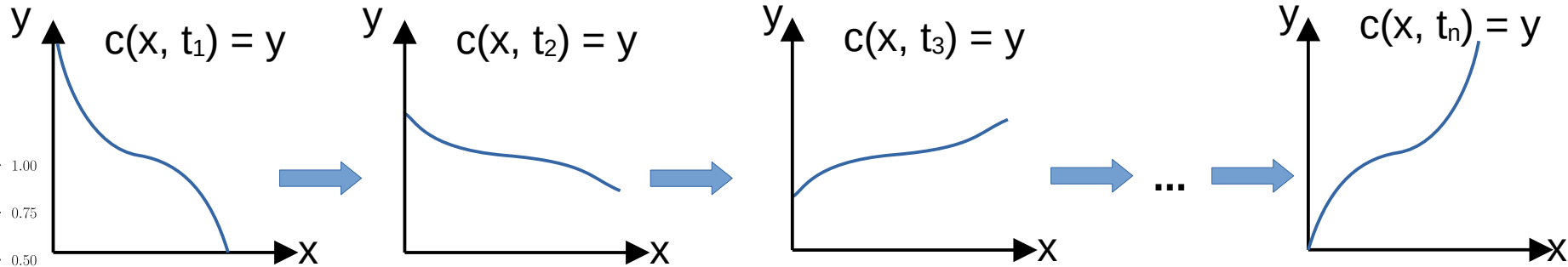


Outlook

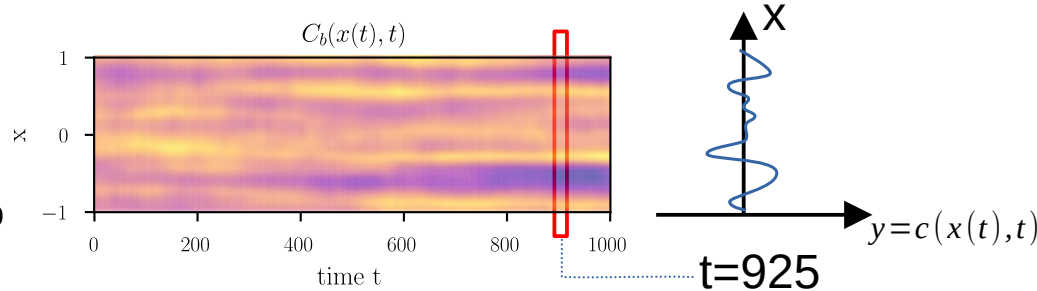


Problem Statement

■ Concept Drift


 $c(x(t), t)$

The value of y corresponds to the color.



Problem Statement



Related Work



Our Method



Evaluation

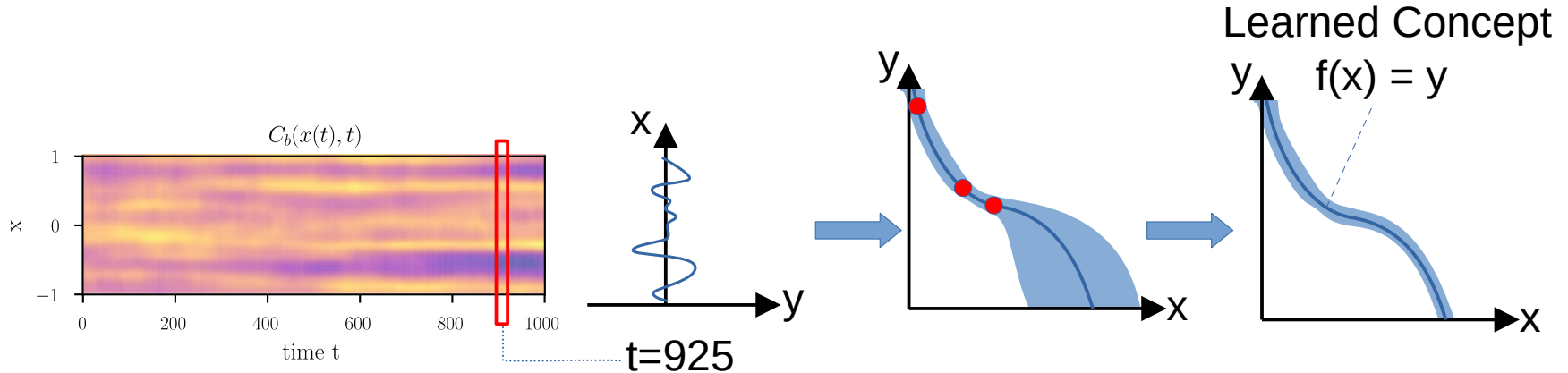


Outlook



Problem Statement

- The Challenge for Active Learning for Regression under Concept Drift:



- Once uncertainty is low, method stops measuring and learning unaware of drift.
→ Method gets stuck.
- There is no way to detect a obsolete concept without expensive measurement of the target (such measurements are no longer performed).

Problem Statement (summary)

■ Concept Drift:

- The learned function (concept) becomes obsolete after some time.

■ Active Learning:

- There is no way to detect a obsolete concept without measuring the target.
- Measuring the target is expensive.

■ User Requirement:

- A user requires estimations for which estimation errors are below a “threshold of usefulness”
- Estimations with higher error are harmful to follow-up tasks.
(Think of crops planted in supposedly good soil that all die because of bad soil quality)

Research question

Concept Drift

Expensive Measurements

Require low estimation errors



Problem Statement



Related Work



Our Method



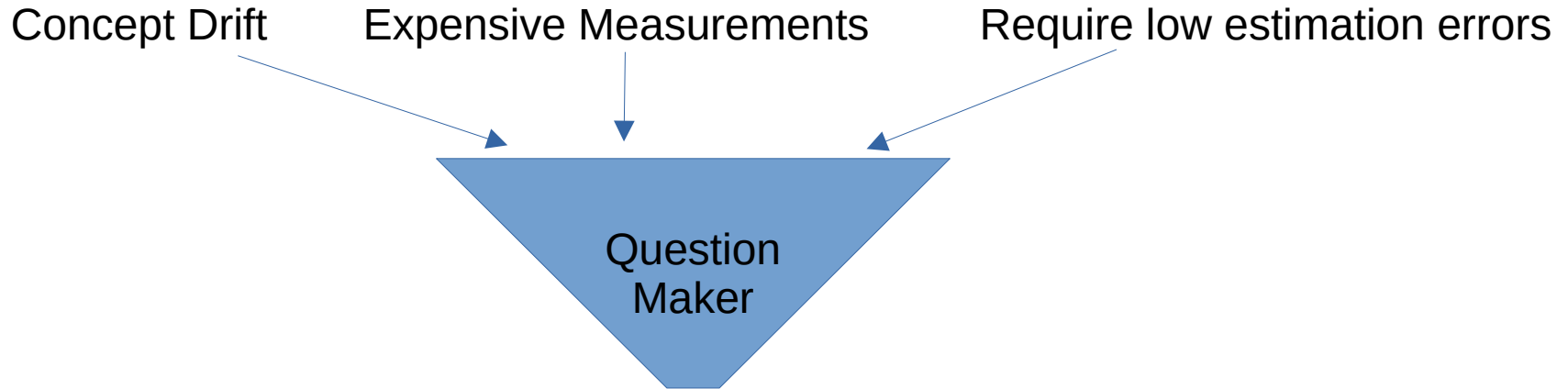
Evaluation



Outlook



Research question



How can we decide how often to measure the target
(adapt the measurement frequency)

while:

Keeping the number of measurements to a minimum,
Keeping prediction errors below a user-required threshold?

Problem Statement



Related Work



Our Method



Evaluation



Outlook



Research question

Concept Drift

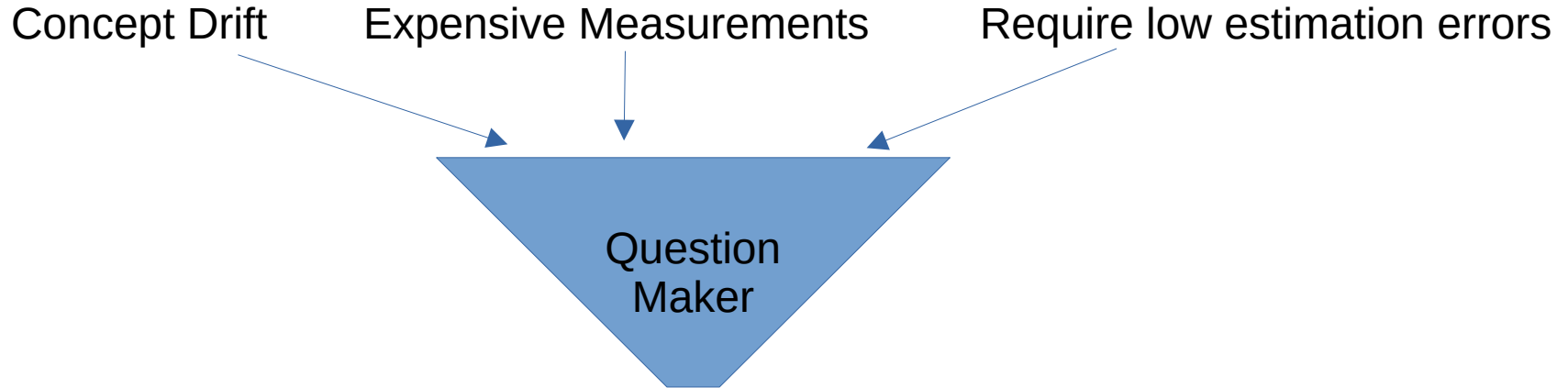
Expensive Measurements

Require low estimation errors



Adapt measurement frequency.
Minimize expensive measurements.
Satisfy user-required threshold.

Related Work



Adapt measurement frequency.
Minimize expensive measurements.
Satisfy user-required threshold.

**Related work answers some of these points separately,
but has no answer for all in combination!**

Problem Statement



Related Work



Our Method



Evaluation



Outlook



Related Work (summary)

	Active learning for regression	Concept drift (no active learning)	Active learning for classification with drift	Methods in practice
Adapt measurement frequency:	✗	✗		✗
Minimize expensive measurements:		✗		✗
Satisfy user-required threshold:	✗		✗	✗

Problem Statement



Related Work



Our Method



Evaluation



Outlook



Our Method

	Our Method
Adapt measurement frequency:	
Minimize expensive measurements:	
Satisfy user-required threshold:	

Problem Statement



Related Work



Our Method



Evaluation

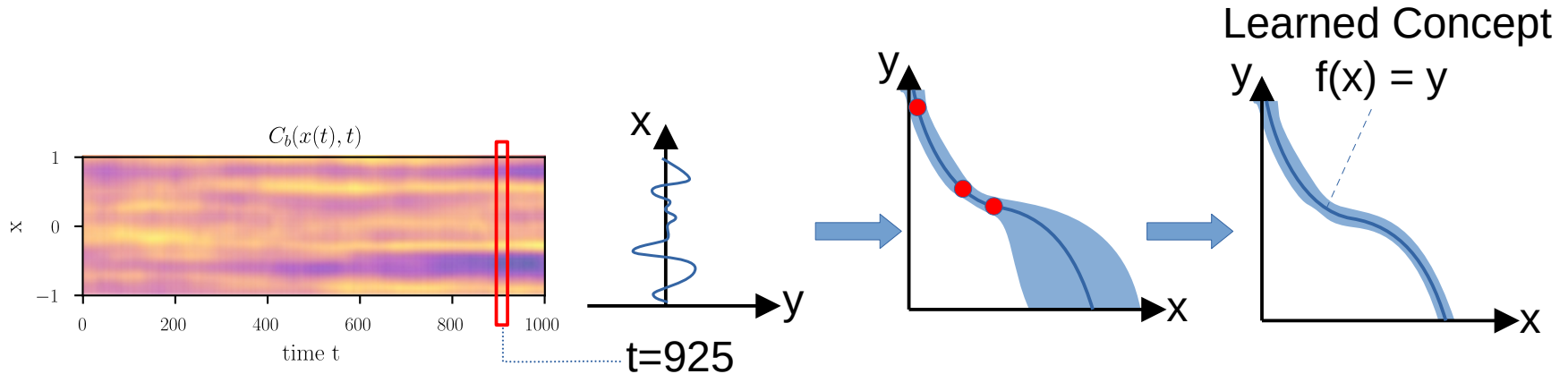


Outlook



Our Method

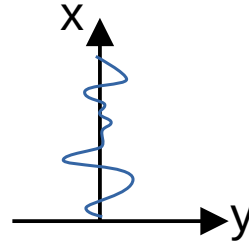
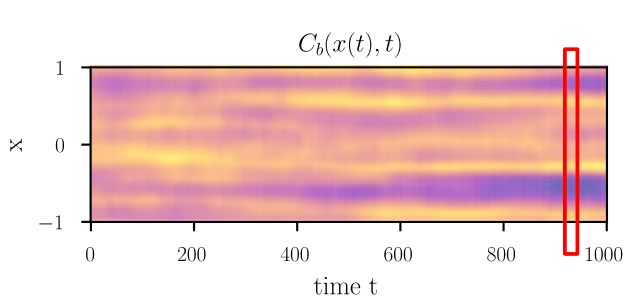
Remember: Active Learning without considered drift:



Once uncertainty is low, method stops learning unaware of drift.
 → Method gets stuck.

Our Method

- We need to increase the uncertainty again! (preventing getting stuck)
- We learn statistics about the drift behavior:



Problem Statement



Related Work



Our Method



Evaluation

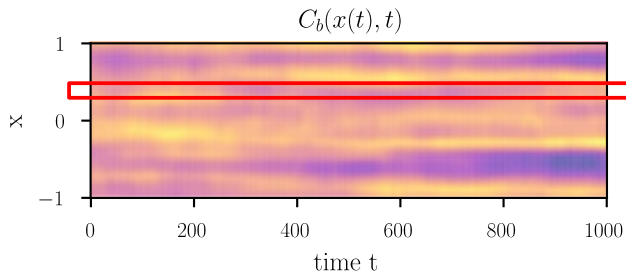


Outlook



Our Method

- We need to increase the uncertainty again! (prevent getting stuck)
- We learn statistics about the drift behavior:



Problem Statement



Related Work



Our Method



Evaluation

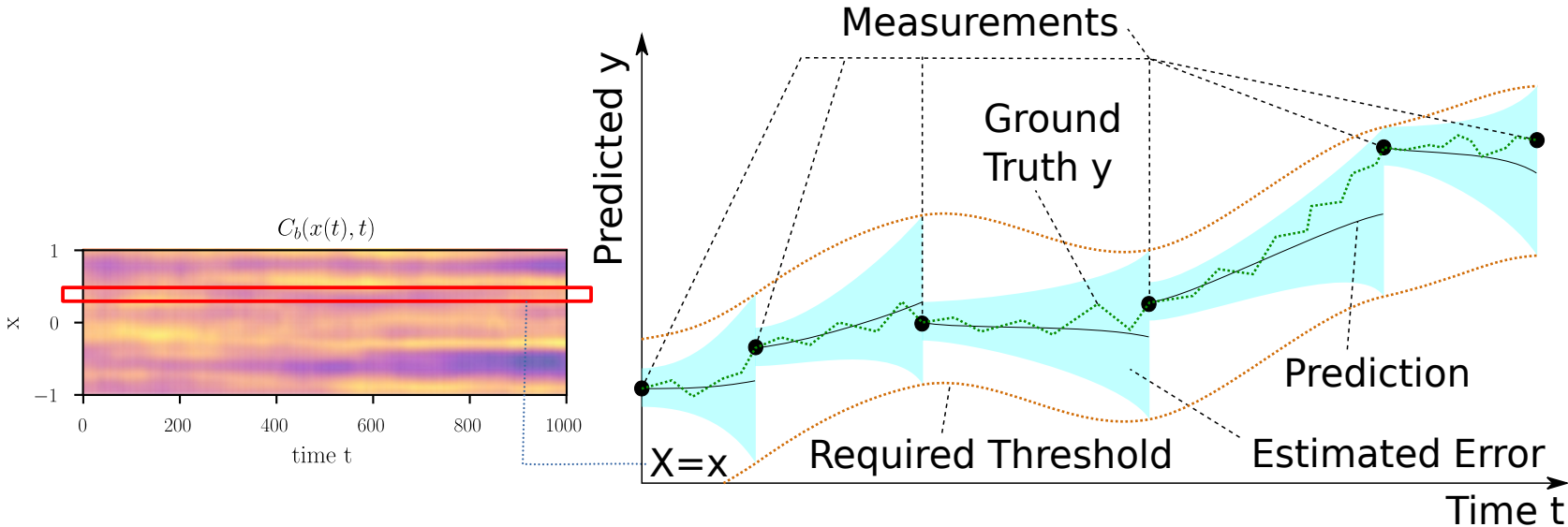


Outlook



Our Method

- We need to increase the uncertainty again! (prevent getting stuck)
- We learn statistics about the drift behavior:



Problem Statement



Related Work



Our Method



Evaluation



Outlook



Our Method

- We use a $N + 1$ dimensional Gaussian Process Model.
- $N [1 \dots 5]$ dimensions for the Input Stream X .
- 1 dimension for the time t .

- To model the increasing uncertainty over time we use a Brownian kernel $B(t)$.
- We use an RBF kernel $I(t)$ for modeling the input-target relation.
- We use an RBF kernel $W(t)$ for weighting / quantifying how much impact the drift has on the output y for a given input x .

$$C(x, t) = I(x) + W(x)B(t)$$

Our Method

■ Details:

- We perform measurements once the estimated uncertainty reaches the user-required threshold.
- We recalibrate the Gaussian Process Model using the measurement history and the new measurement.

Evaluation

- We evaluate on five datasets commonly used for classification and adapted them to regression.
- We evaluate on input streams with dimensions 1...5.
- We compare against four baseline:
 - Consecutive Measurement (as used in practice).
 - Classic Active Learning (not considering drift).
 - A change detection approach AAIL [24] (adapted from classification).
 - A second change detection approach considering detection errors.
- We evaluate each approach and each parameter configuration 50 times.

Problem Statement



Related Work



Our Method



Evaluation



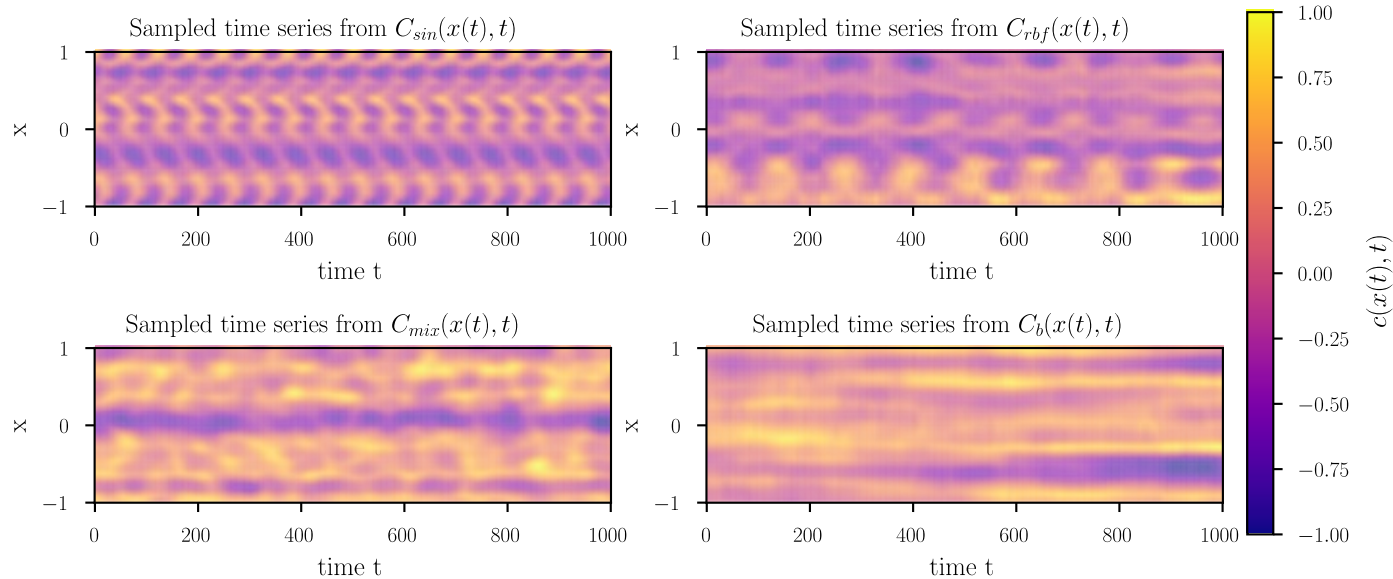
Outlook



Evaluation

■ Example one dimensional data:

Time series sampled from different priors



Problem Statement



Related Work



Our Method



Evaluation

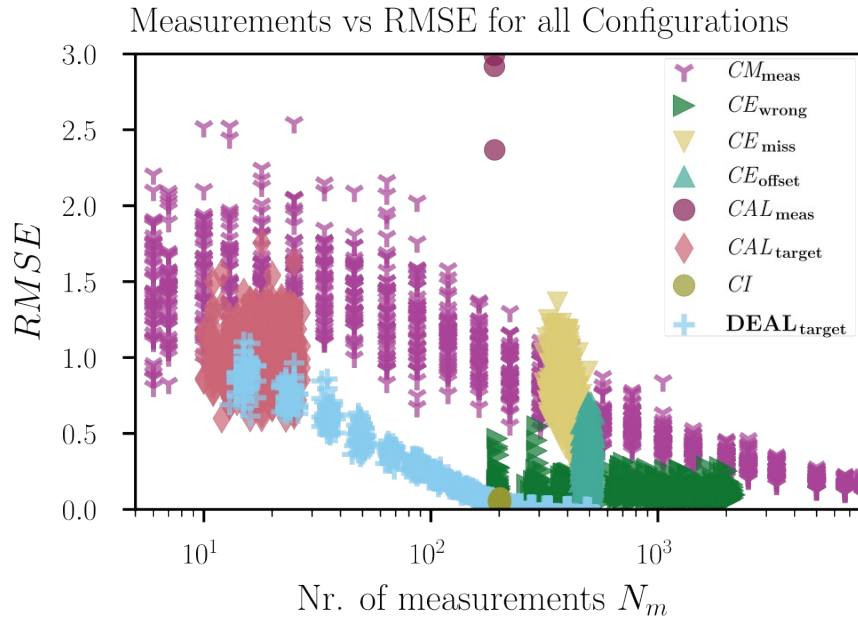


Outlook



Evaluation

Results



Problem Statement



Related Work



Our Method



Evaluation



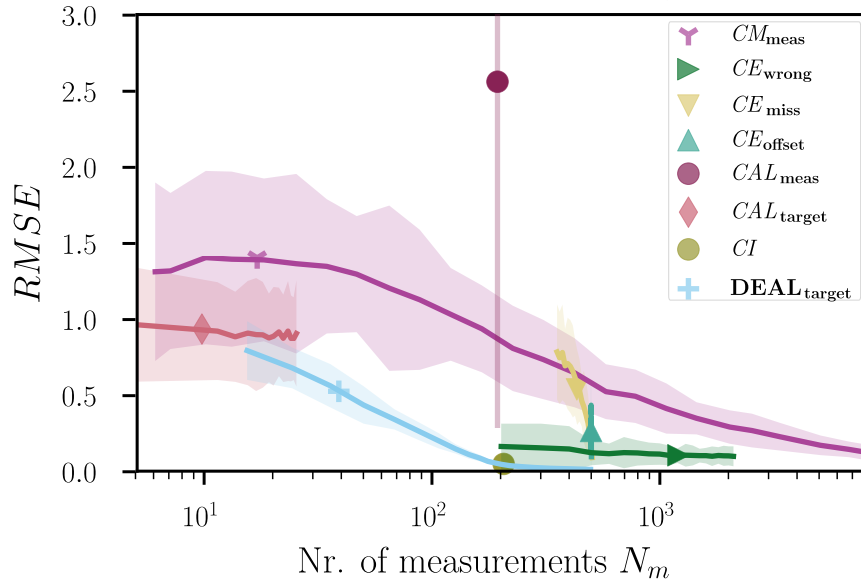
Outlook



Evaluation

Results

Measurements vs RMSE for all Configurations



Problem Statement



Related Work



Our Method



Evaluation

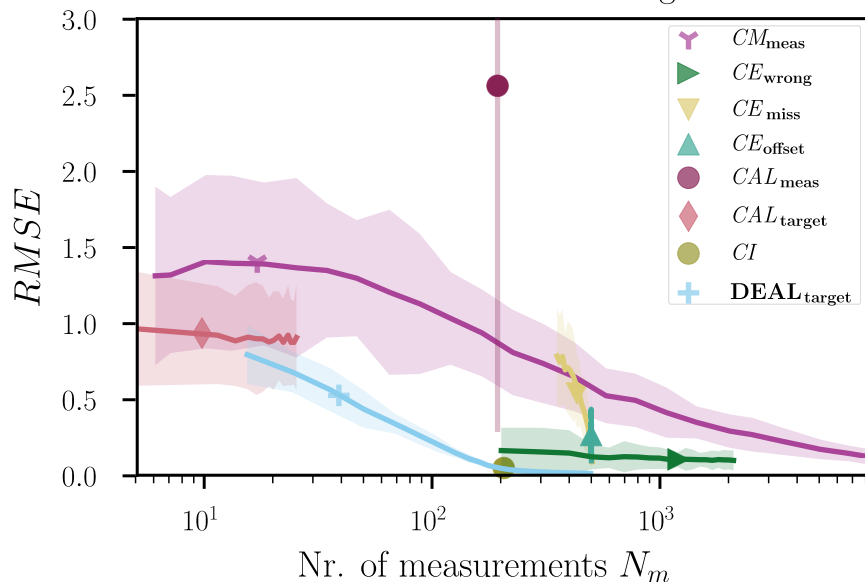


Outlook



Results

Measurements vs RMSE for all Configurations



Only DEAL and CM enable control of the user-required maximal error.

Problem Statement



Related Work



Our Method



Evaluation



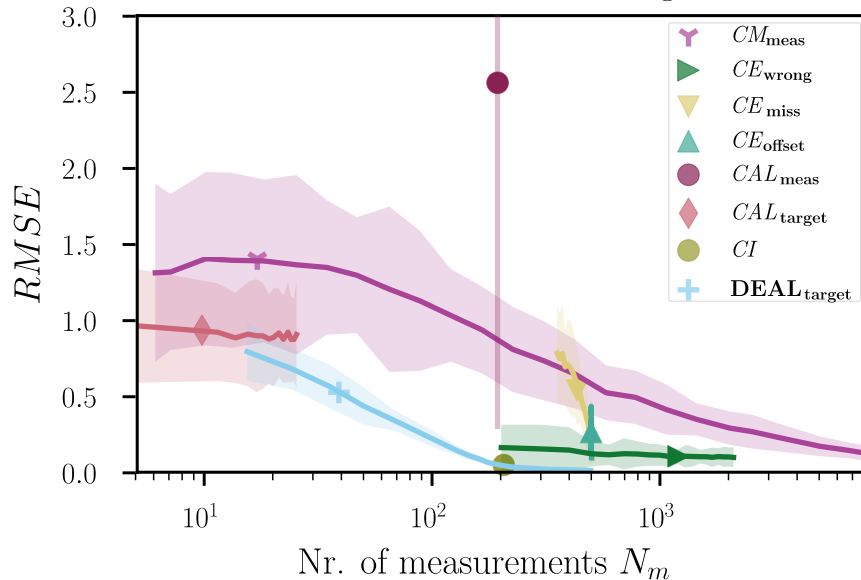
Outlook



Evaluation

Results

Measurements vs RMSE for all Configurations



- Only DEAL and CM enable control of the user-required maximal error.
- Over all datasets DEAL has the most stable performance.

Problem Statement



Related Work



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Evaluation



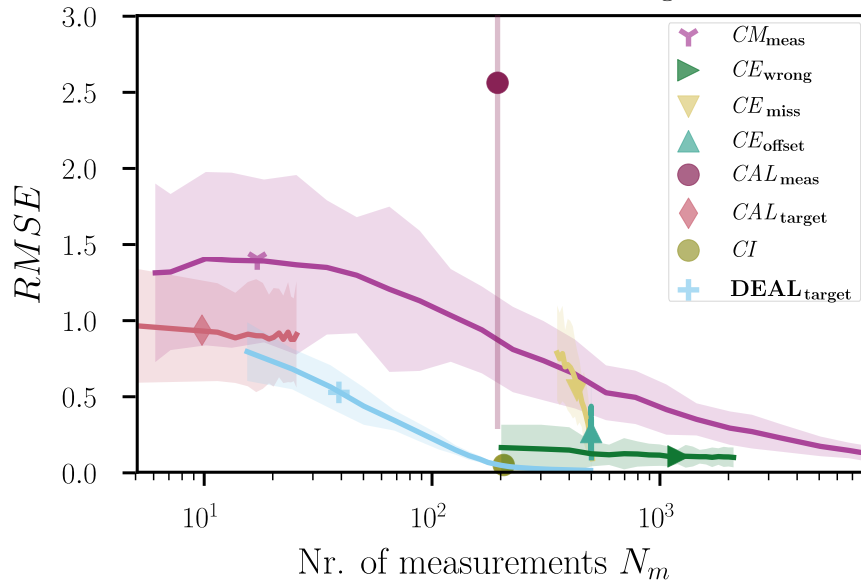
Outlook



Evaluation

Results

Measurements vs RMSE for all Configurations



- Only DEAL and CM enable control of the user-required maximal error.
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Problem Statement



Related Work



Our Method



Evaluation

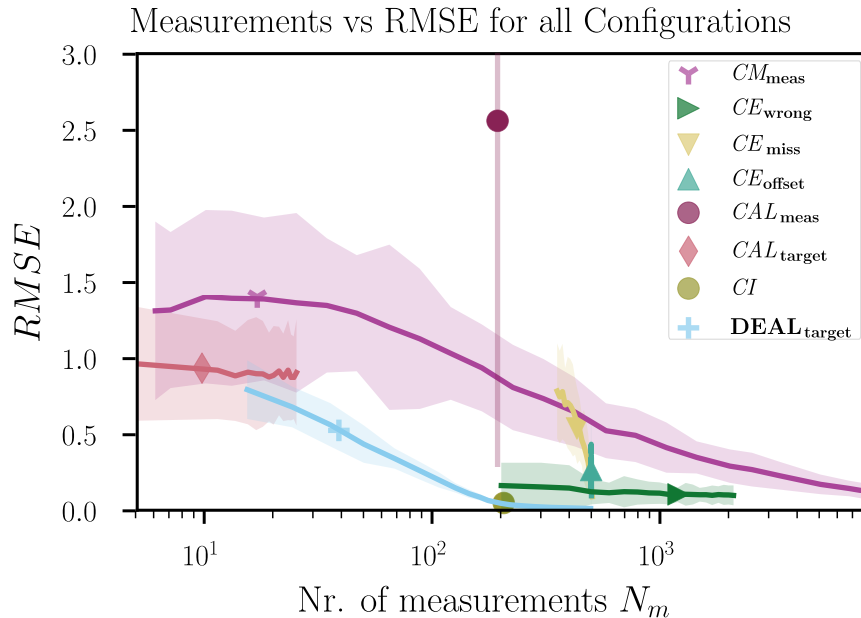


Outlook



Evaluation

Results



- Only DEAL and CM enable control of the user-required maximal error.
- Over all datasets DEAL has the most stable performance.
 - DEAL automatically adapts measurement frequency.
- For a given error-threshold DEAL requires on average, 20 times fewer measurements.

Problem Statement



Related Work



Our Method



Evaluation



Outlook



Conclusion

■ Challenges:

- The relationship between input and target variables may drift due to environmental influences that are not observed.
- Current work on active learning does not consider this for continuous variables.

■ Our Contribution:

- We proposed DEAL, a method that satisfies a given user-required prediction error threshold by adapting its measurement frequency to the drifting relationship.
- DEAL requires, on average, 20 times fewer measurements than methods used in practice.
- DEAL automatically adapts to changing drift behavior, preventing model degradation and improper set parameters.

Problem Statement



Related Work



Our Method



Evaluation



Outlook



References

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Problem Statement



Related Work



Our Method



Evaluation



Outlook



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Problem Statement



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Our Method



Evaluation



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DEAL: Data-Efficient Active Learning for regression under drift

A First Method Aimed at the Gap of Regression Active Learning with Drift

